

Single Higgs Precision at a Muon Collider

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with Patrick Meade

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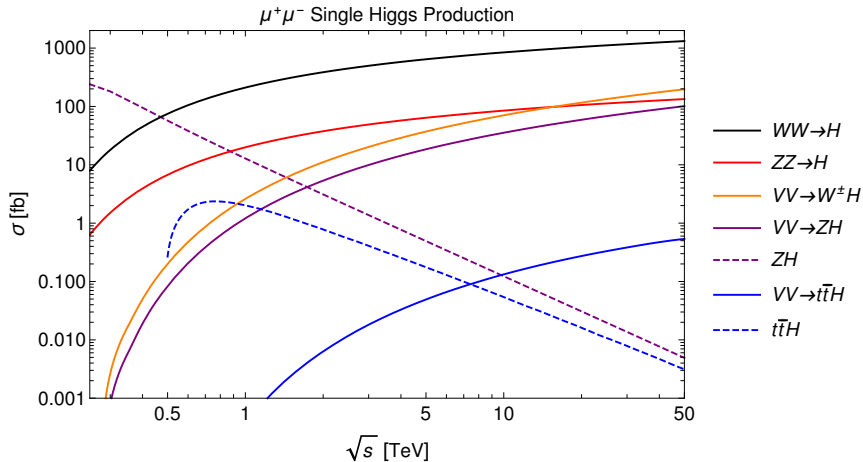
December 15, 2022

The current status (J. de Blas et al. 1905.03764)

κ -0:
 $BR_{BSM} = 0$
 $\kappa_i \equiv g_i/g_i^{SM}$

κ -0 fit	HL- LHC	LHeC	HE-LHC S2 S2'	ILC 250 500 1000			CLIC 380 1500 3000			CEPC	FCC-ee 240 365		FCC-ee/ eh/hh
κ_W	1.7	0.75	1.4 0.98	1.8	0.29	0.24	0.86	0.16	0.11	1.3	1.3	0.43	0.14
κ_Z	1.5	1.2	1.3 0.9	0.29	0.23	0.22	0.5	0.26	0.23	0.14	0.20	0.17	0.12
κ_g	2.3	3.6	1.9 1.2	2.3	0.97	0.66	2.5	1.3	0.9	1.5	1.7	1.0	0.49
κ_γ	1.9	7.6	1.6 1.2	6.7	3.4	1.9	98*	5.0	2.2	3.7	4.7	3.9	0.29
$\kappa_{Z\gamma}$	10.	—	5.7 3.8	99*	86*	85*	120*	15	6.9	8.2	81*	75*	0.69
κ_c	—	4.1	— —	2.5	1.3	0.9	4.3	1.8	1.4	2.2	1.8	1.3	0.95
κ_t	3.3	—	2.8 1.7	—	6.9	1.6	—	—	2.7	—	—	—	1.0
κ_b	3.6	2.1	3.2 2.3	1.8	0.58	0.48	1.9	0.46	0.37	1.2	1.3	0.67	0.43
κ_μ	4.6	—	2.5 1.7	15	9.4	6.2	320*	13	5.8	8.9	10	8.9	0.41
κ_τ	1.9	3.3	1.5 1.1	1.9	0.70	0.57	3.0	1.3	0.88	1.3	1.4	0.73	0.44

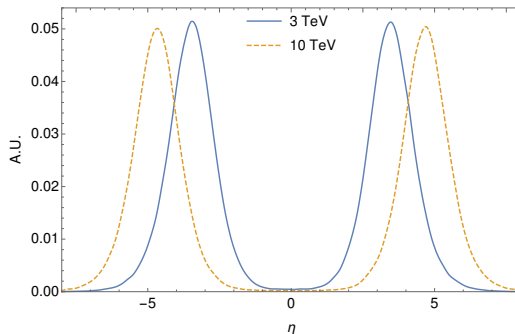
Single Higgs Production at Muon Colliders (2203.09425)



High energies dominated by $WW \rightarrow H$ and $ZZ \rightarrow H$.

Forward Muons

To distinguish between WW -fusion and ZZ -fusion, must be able to tag the forward muons beyond the $|\eta| \approx 2.5$ nozzles



For ZZ -fusion, we include results considering tagging up to $|\eta| \leq 6$.

Event Generation and Detector Assumptions

Event generation is done using MadGraph5 and showering with Pythia8

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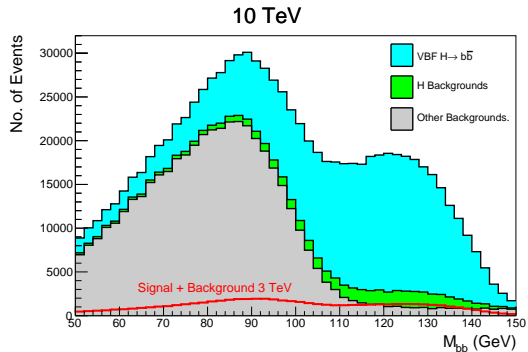
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Without forward tagging, combine WWF and ZZF- otherwise, consider separately

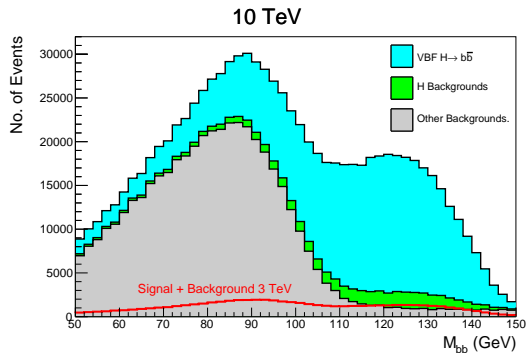
Hadronic Processes: $b\bar{b}$



Precision (%)

Energy	Combination	WWF	ZZF
3 TeV	0.76	0.80	2.6
10 TeV	0.21	0.22	0.77

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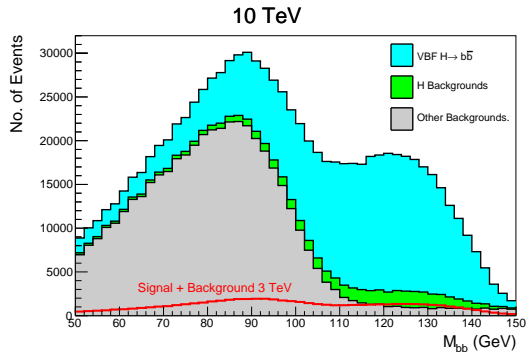


Dominant background from Z-peak:
distinguishing the two is crucial

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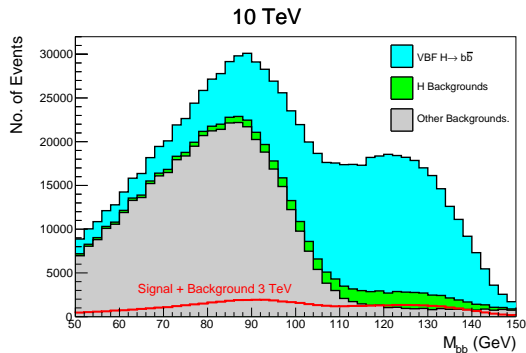
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The $c\bar{c}$ and gg channels are very similar, with
mistagged $H \rightarrow b\bar{b}$ contributing a large
background as well

WW^*, ZZ^*

For WW^* and ZZ^* , we generate the full $2 \rightarrow 6$ backgrounds such as $\mu\mu \rightarrow \nu\nu\ell\ell jj$ using MadGraph.

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Process	Number of Events					
	3 TeV			10 TeV		
	$4j$	$2j2\ell$	4ℓ	$4j$	$2j2\ell$	4ℓ
$\mu^+\mu^- \rightarrow \nu_\mu\bar{\nu}_\mu H; H \rightarrow ZZ^* \rightarrow X$	124	103	5	2910	1590	66
$\mu^+\mu^- \rightarrow \mu^+\mu^- H; H \rightarrow ZZ^* \rightarrow X$	3	9	0	315	151	8
Others	6700	50	0	208000	1370	2

κ -0 Fit Result (With Fwd Tagging) [%]

	3 TeV @ 1 ab ⁻¹	10 TeV @ 10 ab ⁻¹
κ_W	0.37	0.10
κ_Z	1.2	0.34
κ_g	1.6	0.45
κ_γ	3.2	0.84
$\kappa_{Z\gamma}$	21	5.5
κ_C	5.8	1.8
κ_t	34	53
κ_b	0.84	0.23
κ_μ	14	2.9
κ_τ	2.1	0.59

**Assume no BSM
branching ratios**

$$\kappa_i = g_i / g_i^{SM}$$

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Removing forward tagging
mainly affects κ_Z :

- 1.2% \rightarrow 5.1%
- 0.34% \rightarrow 1.4%

Where do we stand? (with forward tags)

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For a width precision of $\Delta\Gamma$, can't obtain a coupling precision better than $\Delta\kappa \sim (1/4)\Delta\Gamma$.

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Let's look in more detail

Measuring σ_{Incl}

At e^+e^- colliders, one measures the inclusive $e^+e^- \rightarrow ZH$ cross section via the recoil mass method:

Assuming one knows E_{CM} , then by kinematics

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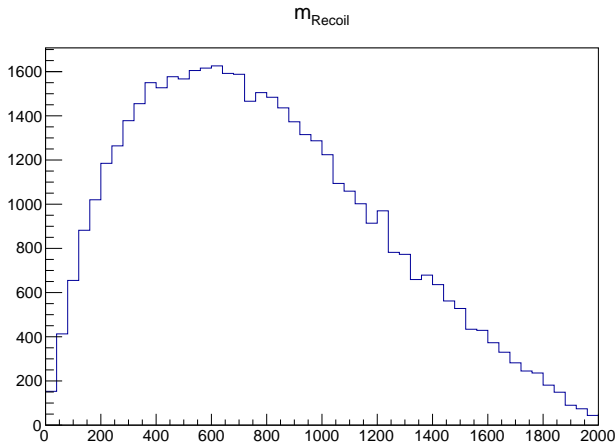
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Nevertheless, could this be done at a muon collider via the forward muons in $\mu^+\mu^-H$?

Can we do this for $\mu^+\mu^- \rightarrow \mu^+\mu^- H$?



Not really... would need unrealistically good energy resolution in forward detectors

LHC techniques

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If $\kappa_V \neq 1$, then $W_L W_L \rightarrow W_L W_L$ scattering grows with energy, $\sigma \propto s^2$

High energy $VV \rightarrow VV$ scattering is highly sensitive to κ_V !

Off-shell $VV \rightarrow VV$ scattering

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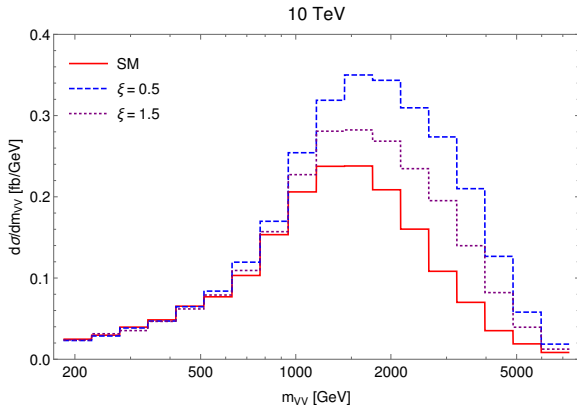
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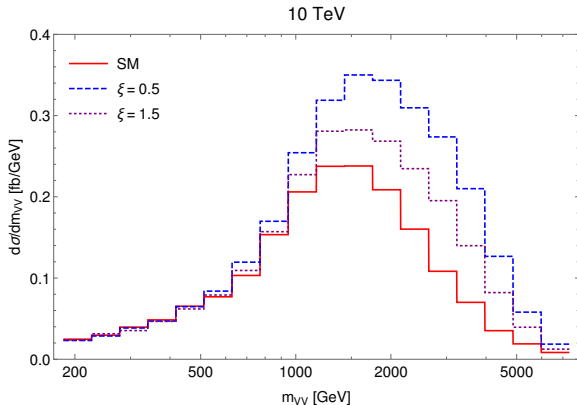
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Fitting κ_W , κ_Z , and ξ yields:

$\Delta\Gamma = 4.0\%$ at 10 TeV

$\Delta\Gamma = 58\%$ at 3 TeV
(not competitive with LHC)

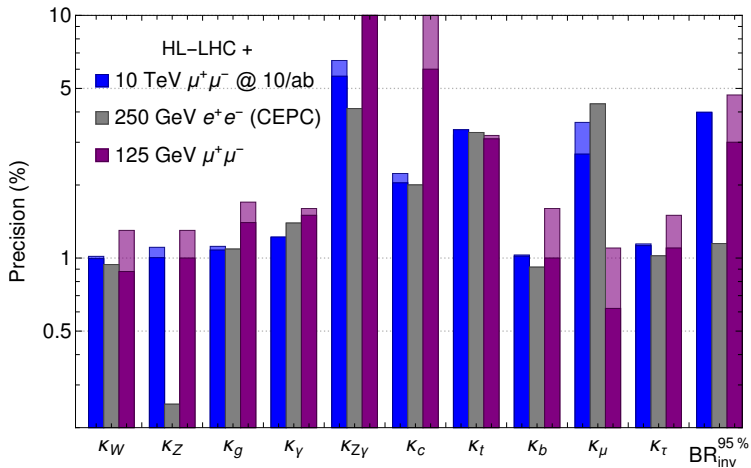


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Comparisons (combined with HL-LHC)

Blue shaded:
forward tagging

Purple shaded:
5 vs 20/ab



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This restoration only occurs above resonance: must be lighter than our off-shell analysis window!

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4. The new physics must be custodially symmetric at tree-level (off-shell loophole)
5. Direct search constraints must be satisfied (both)

Higher multiplet scalars

One of the only ways to generate a $\kappa_V > 1$ is by adding scalar multiplets larger than doublets that contribute to EWSB.

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In either case, there would be many new electroweak charged scalar states lighter than a few TeV to search for directly, which muon colliders are great at!

Searching for light states from $\mu^+\mu^-H$

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Further study necessary to see if this is feasible or not

Searching for light states

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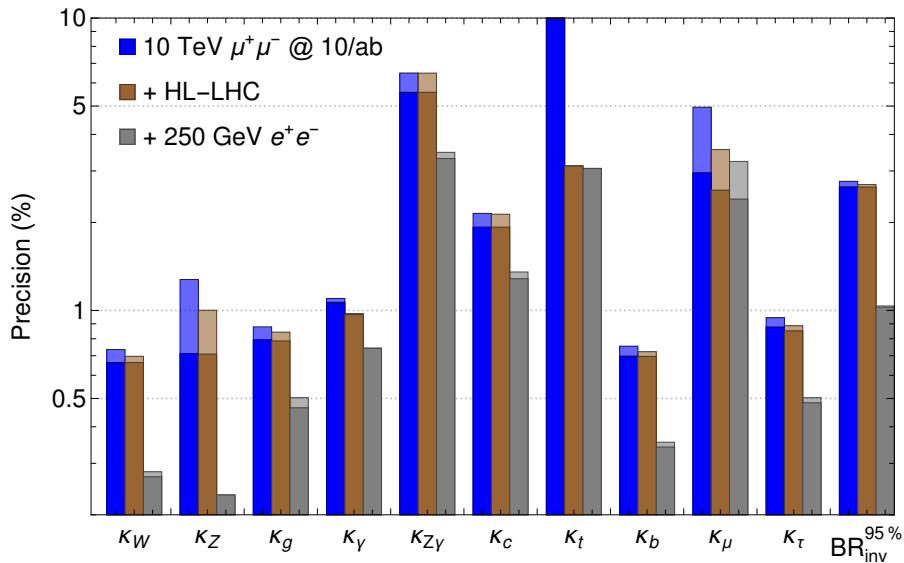
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All depend on κ_W, κ_Z , and BR_{inv} : must do the full fit to see impact

Including this in the fit



Conclusion

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A 3 TeV $\mu^+\mu^-$ collider **cannot** effectively constrain the width, even indirectly, beyond what the LHC can do.

Great complementary between a 10 TeV $\mu^+\mu^-$ collider and e^+e^- or 125 GeV $\mu^+\mu^-$ colliders, since they have different dominant production modes.

BACKUPS

Flavour Tagging

b -tagging is done using the tight working point (50%) inspired by CLIC (1812.07337)

- c -quark mistagging rate $\leq 3\%$
- light quark mistagging rate $\leq 0.5\%$

For c -tagging, we use the tagging rates of ILC reported in (1506.08371). We take 20% as our working point to match the Smasher's Guide.

- b -quark mistagging rate of flat 1.3%
- light quark mistagging rate of flat 0.66%

For $H \rightarrow \tau\tau$, we take a τ -tagging efficiency of 80% with a jet mistag rate of 2%.

Event Selection ($b\bar{b}$, $c\bar{c}$, $gg(+s\bar{s})$)

Apply an additional correction to b -jet p_T to account for energy losses during reconstruction (1811.02572)

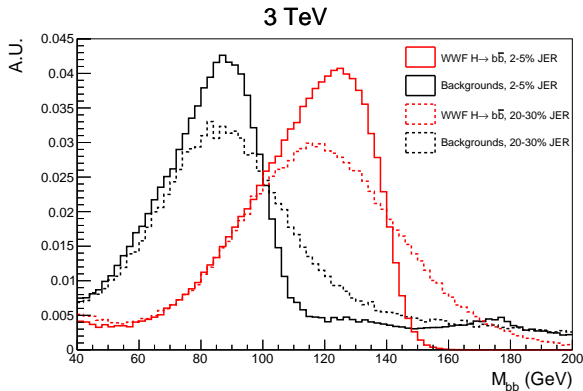
- Smoothly scales 4-momentum by up to ~ 1.16 at low p_T
- Rough approximation to ATLAS $ptcorr$ correction (1708.03299)
- Reproduces a Higgs peak centered near 125 GeV

Apply a similar correction to c -jets

Events that pass the P_T and η cuts are then selected based on an invariant mass cut:

- $100 < M_{b\bar{b}} < 150$ for $b\bar{b}$
- $105 < M_{c\bar{c}} < 145$ for $c\bar{c}$
- $95 < M_{jj} < 135$ for $gg(+s\bar{s})$

Estimating the Effects of the BIB



Worse JER based on current fullsim- additional spreading roughly doubles the background contribution from the Z peak: $0.76\% \rightarrow 0.86\%$ precision, quite comparable to fullsim result (2209.01318).

$$c\bar{c}, gg(+s\bar{s}), \tau^+\tau^-$$

The dominant backgrounds for $c\bar{c}$ and $gg(+s\bar{s})$ are mostly the same as for $b\bar{b}$ and primarily removed via an M_{jj} cut

$H \rightarrow b\bar{b}$ becomes a large irreducible background

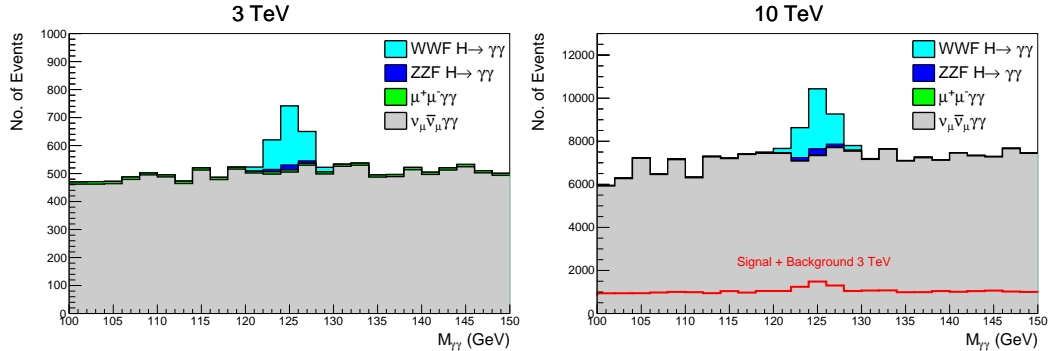
Following the same procedure as in $b\bar{b}$, we obtain results for $c\bar{c}$ and $gg(+s\bar{s})$:

Energy	Precision (%)	
	$c\bar{c}$	$gg(+s\bar{s})$
3 TeV	13	3.3
10 TeV	4.0	0.89

$\tau^+\tau^-$ follows a similar strategy with similar backgrounds, adding $\theta_{\tau\tau} > 15(20)$ cuts, to get 4.0(1.1)% precision.

$\gamma\gamma$ and $Z\gamma$

For $\gamma\gamma$, require no isolated leptons and a cut of $122 < M_{\gamma\gamma} < 128$.



The $Z(jj)\gamma$ process has similar backgrounds as the hadronic modes, but with more complicated cuts.

This process requires special care: VBF at 10 TeV vs s -chan at 3, the cross section is small, and the $t\bar{t}$ background is large.

Select events with four b -tagged $p_T > 20$ jets and ≤ 1 leptons, apply various cuts on $E_{W,t,H}$, $m_{W,t,H}$

Obtain a precision of 61% at 3 TeV and 53% at 10 TeV

(Different y_t dependence at 3 and 10 TeV)

Process	Number of Events			
	3 TeV		10 TeV	
	SL	Had	SL	Had
$t\bar{t}H; H \rightarrow b\bar{b}$	34	63	49	59
$t\bar{t}H; H \not\rightarrow b\bar{b}$	9	21	6	11
$t\bar{t}$	609	2070	502	1440
$t\bar{t}Z$	207	362	530	663
$t\bar{t}b\bar{b}$	9	21	15	18

κ -0 Fit Result [%]

	$\mu^+ \mu^-$		+ HL-LHC		+ HL-LHC + 250 GeV $e^+ e^-$	
	3 TeV	10 TeV	3 TeV	10 TeV	3 TeV	10 TeV
κ_W	0.55	0.16	0.39	0.14	0.33	0.11
κ_Z	5.1	1.4	1.3	0.94	0.12	0.11
κ_g	2.0	0.52	1.4	0.50	0.75	0.43
κ_γ	3.2	0.84	1.3	0.71	1.2	0.69
$\kappa_{Z\gamma}$	24	6.5	24	6.5	4.1	3.5
κ_c	6.8	2.0	6.7	2.0	1.8	1.3
κ_t	35	55	3.2	3.2	3.2	3.2
κ_b	0.97	0.26	0.82	0.25	0.45	0.22
κ_μ	20	4.9	4.6	3.4	4.1	3.2
κ_τ	2.3	0.63	1.2	0.57	0.62	0.41

κ -0 Fit Result [%] with Forward Muon Tagging

	$\mu^+ \mu^-$		+ HL-LHC		+ HL-LHC + 250 GeV $e^+ e^-$	
	3 TeV	10 TeV	3 TeV	10 TeV	3 TeV	10 TeV
κ_W	0.37	0.10	0.35	0.10	0.31	0.10
κ_Z	1.2	0.34	0.89	0.33	0.12	0.11
κ_g	1.6	0.45	1.3	0.44	0.72	0.39
κ_γ	3.2	0.84	1.3	0.71	1.2	0.69
$\kappa_{Z\gamma}$	21	5.5	22	5.5	4.0	3.3
κ_c	5.8	1.8	5.8	1.8	1.7	1.3
κ_t	34	53	3.2	3.2	3.2	3.2
κ_b	0.84	0.23	0.80	0.23	0.44	0.21
κ_μ	14	2.9	4.7	2.5	4.0	2.4
κ_τ	2.1	0.59	1.2	0.55	0.61	0.40

10 TeV @ 10 ab⁻¹: κ -0 Fit Result [%] Without Fwd Tags

	Signal Only (2103.14043)	With Backgrounds (2203.09425)
κ_W	0.06	0.16
κ_Z	0.23	1.4
κ_g	0.15	0.52
κ_γ	0.64	0.84
$\kappa_{Z\gamma}$	1.0	6.5
κ_c	0.89	2.0
κ_t	6.0	55
κ_b	0.16	0.26
κ_μ	2.0	4.9
κ_τ	0.31	0.63

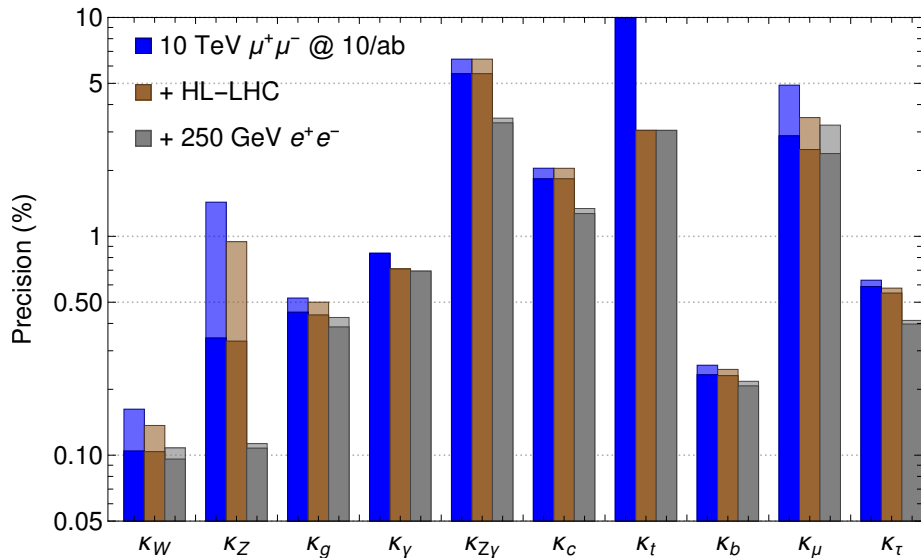
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κ_γ	0.64	0.84
$\kappa_{Z\gamma}$	1.0	5.5
κ_c	0.89	1.8
κ_t	6.0	53
κ_b	0.16	0.23
κ_μ	2.0	2.9
κ_τ	0.31	0.59

Where do we stand? (without forward tags)

κ -0	HL-	LHeC	HE-LHC	ILC			CLIC			CEPC	FCC-ee		FCC-ee/	$\mu^+\mu^-$
fit	LHC		S2 S2'	250	500	1000	380	1500	3000		240	365	eh/hh	3000 10000
κ_W	1.7	0.75	1.4 0.98	1.8	0.29	0.24	0.86	0.16	0.11	1.3	1.3	0.43	0.14	0.55 0.16
κ_Z	1.5	1.2	1.3 0.9	0.29	0.23	0.22	0.5	0.26	0.23	0.14	0.20	0.17	0.12	5.1 1.4
κ_g	2.3	3.6	1.9 1.2	2.3	0.97	0.66	2.5	1.3	0.9	1.5	1.7	1.0	0.49	2.0 0.52
κ_γ	1.9	7.6	1.6 1.2	6.7	3.4	1.9	98★	5.0	2.2	3.7	4.7	3.9	0.29	3.2 0.84
$\kappa_{Z\gamma}$	10.	—	5.7 3.8	99★	86★	85★	120★	15	6.9	8.2	81★	75★	0.69	24 6.5
κ_c	—	4.1	— —	2.5	1.3	0.9	4.3	1.8	1.4	2.2	1.8	1.3	0.95	6.8 2.0
κ_t	3.3	—	2.8 1.7	—	6.9	1.6	—	—	2.7	—	—	—	1.0	35 55
κ_b	3.6	2.1	3.2 2.3	1.8	0.58	0.48	1.9	0.46	0.37	1.2	1.3	0.67	0.43	0.97 0.26
κ_μ	4.6	—	2.5 1.7	15	9.4	6.2	320★	13	5.8	8.9	10	8.9	0.41	20 4.9
κ_τ	1.9	3.3	1.5 1.1	1.9	0.70	0.57	3.0	1.3	0.88	1.3	1.4	0.73	0.44	2.3 0.63

κ -0 Fit



Full list of cuts: off-shell analysis

For $4j$, same cuts at 3 and 10 TeV:

- $p_{T_j} > 60$ GeV, $|\eta_j| < 2.5$, $30 < m_V^{min} < 100$ GeV, $40 < m_V^{max} < 115$ GeV

For $\ell^+ \ell^- jj$:

- $p_{T_{\ell,j}} > 20$ GeV, $|\eta_{j,\ell}| < 2.5$, $70 < m_{\ell\ell} < 115$ GeV, $40 < m_{jj} < 115$ GeV
- $\theta_{\ell\ell}, \theta_{jj} < 25^\circ$ (10 TeV)

For $\ell^\pm \nu_\ell jj$:

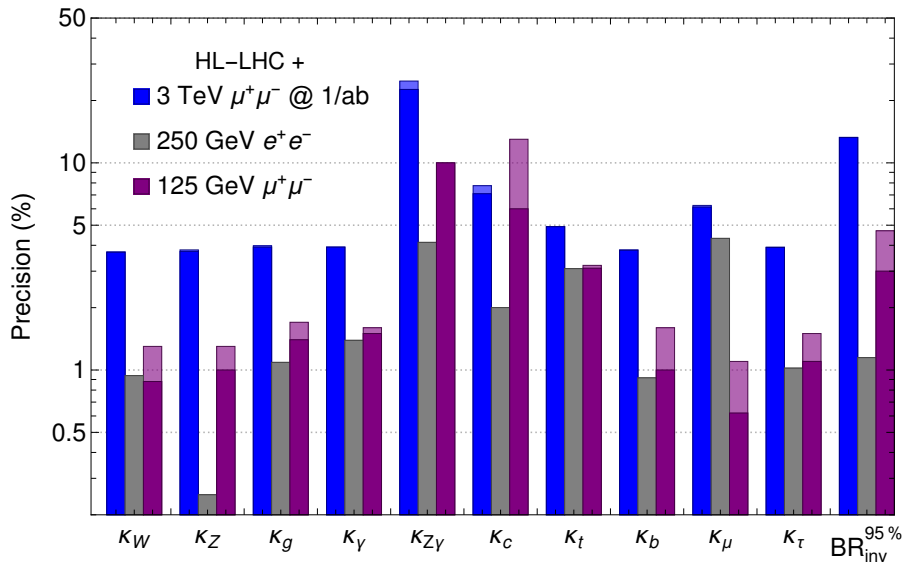
3 TeV:

- $p_{T_{\ell,j}} > 20$ GeV, $|\eta_{j,\ell}| < 2.5$, $p_{T_\ell} < 200$ GeV, $p_{T_{jj}} < 500$ GeV, $40 < m_{jj} < 115$ GeV

10 TeV:

- $p_{T_{\ell,j}} > 20$ GeV, $|\eta_{j,\ell}| < 2.5$, $p_{T_\ell} < 750$ GeV, $p_{T_{jj}} < 1200$ GeV, $40 < m_{jj} < 115$ GeV

Comparisons combined with HL-LHC



Perturbative unitarity

There is a delicate cancellation between the Higgs diagrams and the W/Z continuum diagrams that prevents the longitudinal pieces from growing like $\mathcal{M} \sim E^2$

In extended scalar sectors, this requirement becomes a sum rule for each process

$$(\kappa_{VV}^h)^2 + \sum_i \alpha_i (\kappa_{VV}^i)^2 = 1$$

For example, for the Georgi-Machacek model, $W_L^+ W_L^- \rightarrow W_L^+ W_L^-$ yields

$$(\kappa_W^h)^2 + (\kappa_W^H)^2 + (\kappa_W^{H_5^0})^2 - (\kappa_W^{H_5^{++}})^2 = 1$$

Therefore if m_H and m_5 are below our off-shell analysis window, everything appears the same as in the SM, even if $\kappa_V \neq 1$.

Georgi-Machacek Model

Add to the SM two scalar triplets in a custodial bi-triplet

$$X = \begin{pmatrix} \chi^{0*} & \xi^+ & \chi^{++} \\ -\chi^{+*} & \xi^0 & \chi^+ \\ \chi^{++*} & -\xi^{+*} & \chi^0 \end{pmatrix}$$

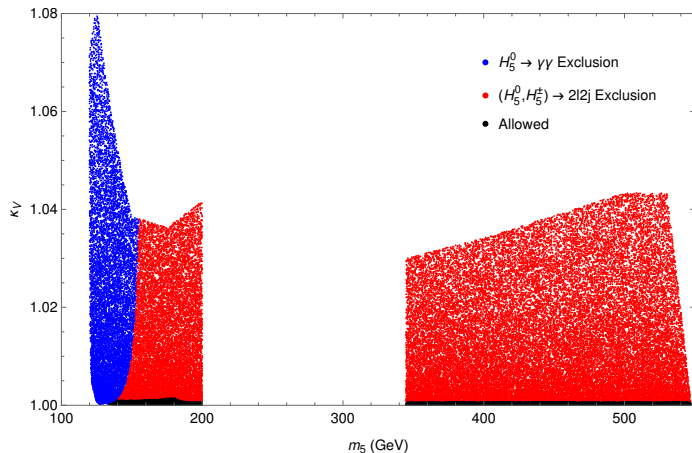
This is custodially symmetric if $\langle \chi^0 \rangle = \langle \xi^0 \rangle$.

After SSB, obtain a custodial fiveplet, a triplet, and two singlets

$$(H_5^0, H_5^\pm, H_5^{\pm\pm}), (H_3^0, H_3^\pm), h, H$$

where the fiveplet does not couple to fermions. For simplicity, we will consider the “low- m_5 ” benchmark, in which all $\kappa_V > 1$ and $m_5 \lesssim 550$ GeV

Constraining the GM model (using GMDCalc)



Expected constraint of $\kappa_V \lesssim 1.002$ from direct searches in low- m_5 benchmark

Georgi-Machacek model

Most general scalar potential with the added field content:

$$\begin{aligned} V(\Phi, X) = & \frac{\mu_2^2}{2} \text{Tr}(\Phi^\dagger \Phi) + \frac{\mu_3^2}{2} \text{Tr}(X^\dagger X) + \lambda_1 \text{Tr}[(\Phi^\dagger \Phi)]^2 + \lambda_2 \text{Tr}(\Phi^\dagger \Phi) \text{Tr}(X^\dagger X) \\ & + \lambda_3 \text{Tr}(X^\dagger X X^\dagger X) + \lambda_4 \text{Tr}[(X^\dagger X)]^2 - \lambda_5 \text{Tr}(\Phi^\dagger \tau_a \Phi \tau_b) \text{Tr}(X^\dagger t_a X t_b) \\ & - M_1 \text{Tr}(\Phi^\dagger \tau_a \Phi \tau_b) (UXU^\dagger)_{ab} - M_2 \text{Tr}(X^\dagger t_a X t_b) (UXU^\dagger)_{ab} \end{aligned}$$

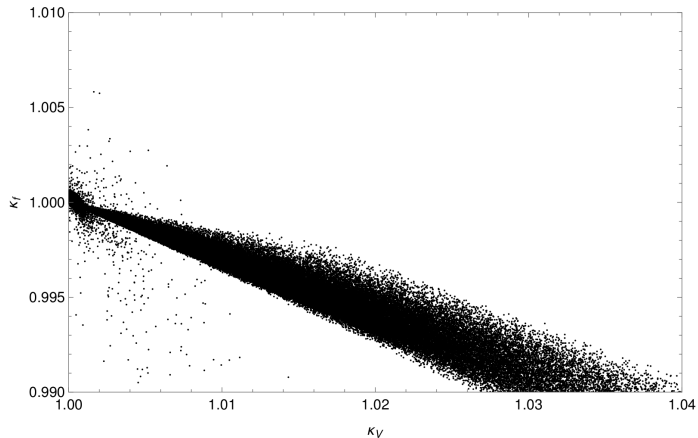
Model with a Z_2 symmetry would be ruled out by HL-LHC (de Lima, Logan, 2209.08393)

Higgs couplings straightforwardly given by

$$\kappa_f = \frac{\cos \alpha}{\cos \theta}, \quad \kappa_V = \cos \alpha \cos \theta - \sqrt{\frac{8}{3}} \sin \alpha \sin \theta$$

with α the $h - H$ mixing angle, and $\cos \theta = \frac{v_\phi}{v}$ the SM Higgs doublet contribution to EWSB.

Constraining the GM model: general scan



Essentially no allowed points with $\kappa_V = \kappa_f > 1$ after expected direct search constraints

Full list of cuts: BR_{inv}

For γH , and $W^\pm H \rightarrow \ell^\pm \nu_\ell H$, only one observed particle, so only one set of cuts:

- $p_{T_{\gamma,\ell}} > 40 \text{ GeV}$, $|\eta_{\gamma,\ell}| < 2.5$

For $ZH \rightarrow \ell^+ \ell^- H$:

- $p_{T_\ell} > 20 \text{ GeV}$, $|\eta_\ell| < 2.5$, $80 < m_{\ell\ell} < 100 \text{ GeV}$, $R_{\ell\ell} > 0.2$

For $VH \rightarrow jjH$:

- $p_{T_j} > 40 \text{ GeV}$, $|\eta_j| < 2.5$, $60 < m_{jj} < 100 \text{ GeV}$

For $\mu^+ \mu^- H$ (forward tagging, only 10 TeV):

- $p_{T_\mu} > 20 \text{ GeV}$, $p_{T_{\mu\mu}} > 100 \text{ GeV}$, $R_{\mu\mu} > 9$, $m_{\mu\mu} > 8000 \text{ GeV}$